



# Auth. Key Exchange

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# Review: key exchange

Alice and Bank want to generate a secret key

- Saw key exchange secure against eavesdropping



- This lecture: **Authenticated Key Exchange (AKE)**  
key exchange secure against active adversaries

# Active adversary

Adversary has complete control of the network:

- Can modify, inject and delete packets
- Example: man-in-the-middle



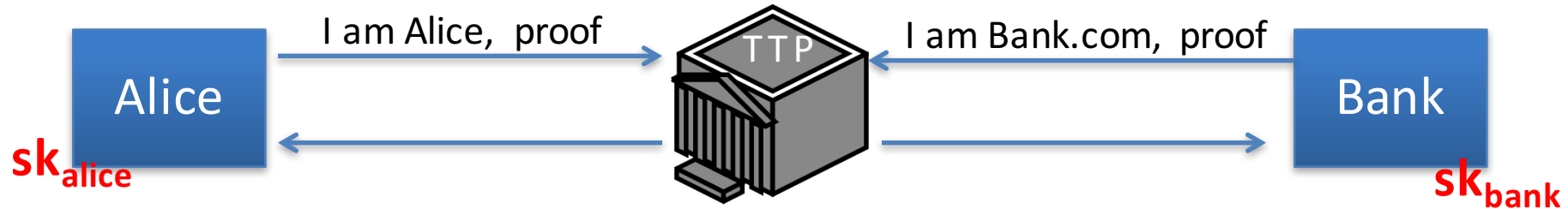
Moreover, some users are honest and others are corrupt

- Corrupt users are controlled by the adversary
  - Key exchange with corrupt users should not “affect” other sessions
- Adversary may corrupt an honest user at time  $T$ 
  - We want sessions established at time  $t < T$  to remain “secure”

# Trusted Third Party (TTP)

All AKE protocols require a TTP to certify user identities.

Registration process:

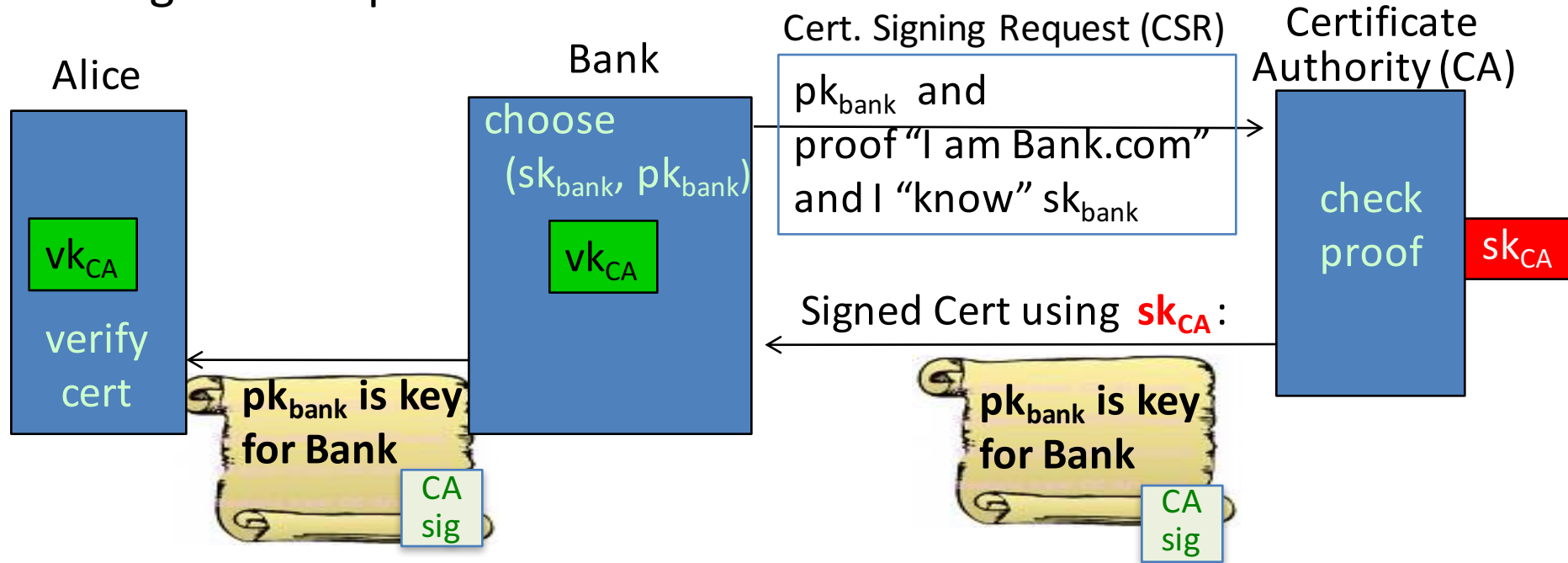


Two types of TTP:

- **Online TTP:** actively participates in every key exchange (Kerberos)  
Benefit: security using only symmetric crypto
- **Offline TTP (CA):** contacted only during registration (... not quite true)

# Offline TTP: Certificate Authority (CA)

Registration process:



- Assumptions:
- all parties have a certified  $pk$  (even corrupt users) (for now)
  - only Bank can get a CA certificate for Bank


# Certificates: example

## Important fields:

<b>Serial Number</b>	5814744488373890497	←
<b>Version</b>	3	
<b>Signature Algorithm</b>	SHA-1 with RSA Encryption ( 1.2.840.113549.1.1.5 )	
<b>Parameters</b>	none	
<b>Not Valid Before</b>	Wednesday, July 31, 2013 4:59:24 AM Pacific Daylight Time	
<b>Not Valid After</b>	Thursday, July 31, 2014 4:59:24 AM Pacific Daylight Time	
<b>Public Key Info</b>		
<b>Algorithm</b>	Elliptic Curve Public Key ( 1.2.840.10045.2.1 )	
<b>Parameters</b>	Elliptic Curve secp256r1 ( 1.2.840.10045.3.1.7 )	
<b>Public Key</b>	65 bytes : 04 71 6C DD E0 0A C9 76 ...	←
<b>Key Size</b>	256 bits	
<b>Key Usage</b>	Encrypt, Verify, Derive	
<b>Signature</b>	256 bytes : 8A 38 FE D6 F5 E7 F6 59 ...	←

Equifax Secure Certificate Authority  
↳ GeoTrust Global CA  
↳ Google Internet Authority G2  
↳ mail.google.com

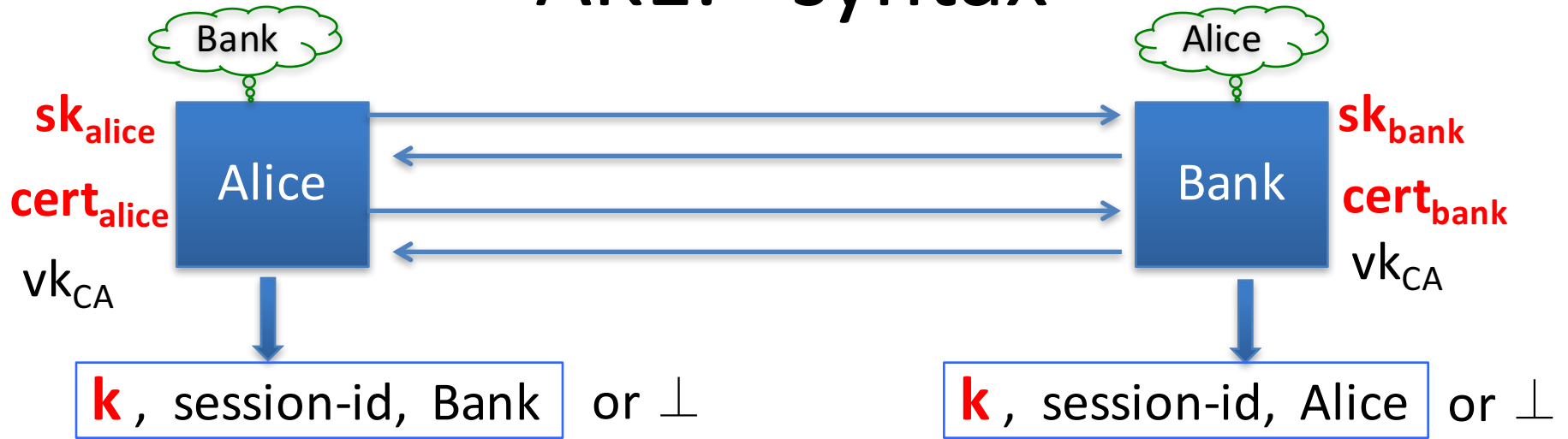
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 **mail.google.com**  
Issued by: Google Internet Authority G2  
Expires: Thursday, July 31, 2014 4:59:24 AM Pacific Daylight Time  
✔ This certificate is valid

▼ **Details**

<b>Subject Name</b>		
<b>Country</b>	US	
<b>State/Province</b>	California	
<b>Locality</b>	Mountain View	
<b>Organization</b>	Google Inc	
<b>Common Name</b>	mail.google.com	←
<b>Issuer Name</b>		
<b>Country</b>	US	
<b>Organization</b>	Google Inc	
<b>Common Name</b>	Google Internet Authority G2	

# AKE: syntax



Followed by Alice sending  $E(k, \text{"data"})$  to Bank

Session-id (sid): public id of session

- Identifies instance of Alice that is talking to instance of Bank

$$sid = sid' \iff k = k'$$

# AKE security (very informal)

Suppose Alice successfully completes an AKE to obtain **(k, sid, Bank)**

If Bank is not corrupt then:

**Authenticity** for Alice: (similarly for Bank)

- If Alice's key  $k$  is shared with anyone, it is only shared with Bank

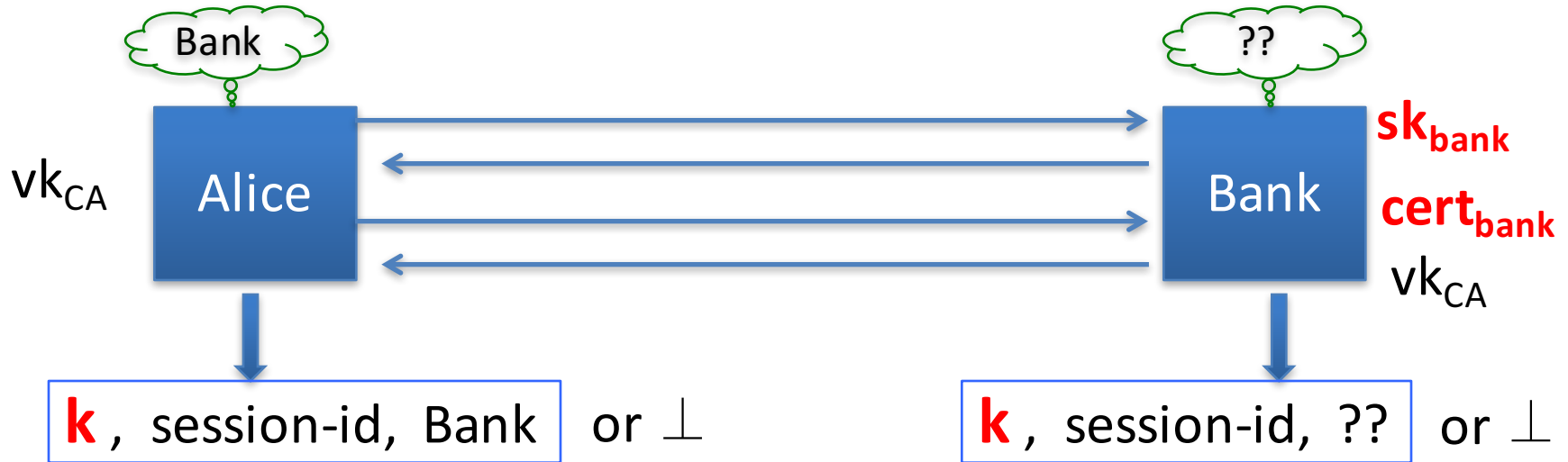
**Secrecy** for Alice: (similarly for Bank)

- To the adversary, Alice's key  $k$  is indistinguishable from random (even if adversary sees keys from other instances of Alice or Bank)

**Consistency**: if Bank completes AKE then it obtains **(k, sid, Alice)**

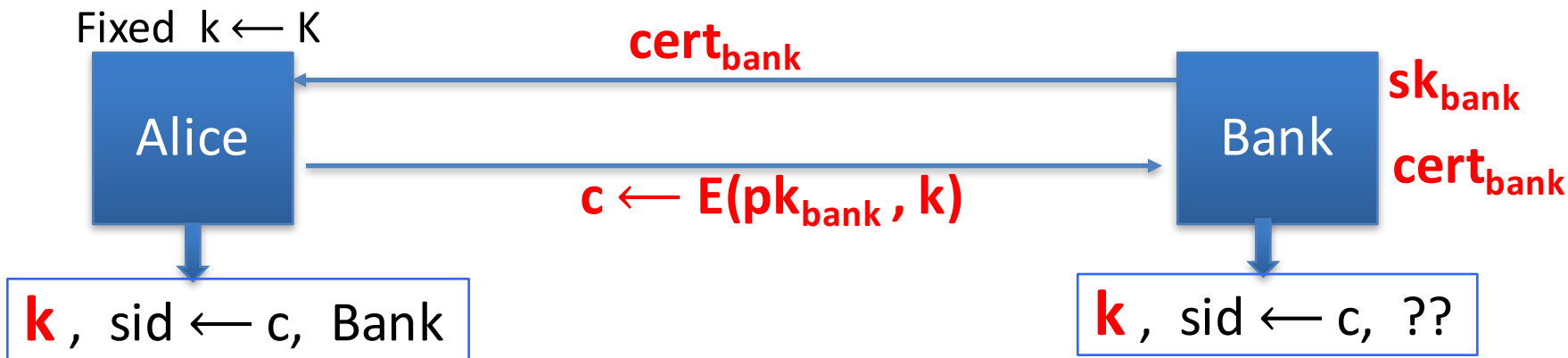


# One-sided AKE



Security: authenticity for Alice and secrecy for Alice

- Bank has no guarantees for identity of peer (no consistency)
- Commonly used on the Web (often followed by ID protocol)



Alice uses same  $k$  for all key exchanges. Is this a secure one-sided AKE?

No, a single AKE with a corrupt user will reveal  $k$

Lots of other problems with this protocol ...

# Things to remember ...

Do not design AKE protocol yourself ...

## Just use latest version of TLS

(sid for TLS is called channel binding)

# Building blocks

**cert<sub>bank</sub>**: contains  $pk_{\text{bank}}$ . Bank has  $sk_{\text{bank}}$ .

$E_{\text{bank}}((m,r)) = E(pk_{\text{bank}}, (m,r))$  where  $E$  is *chosen-ciphertext secure*

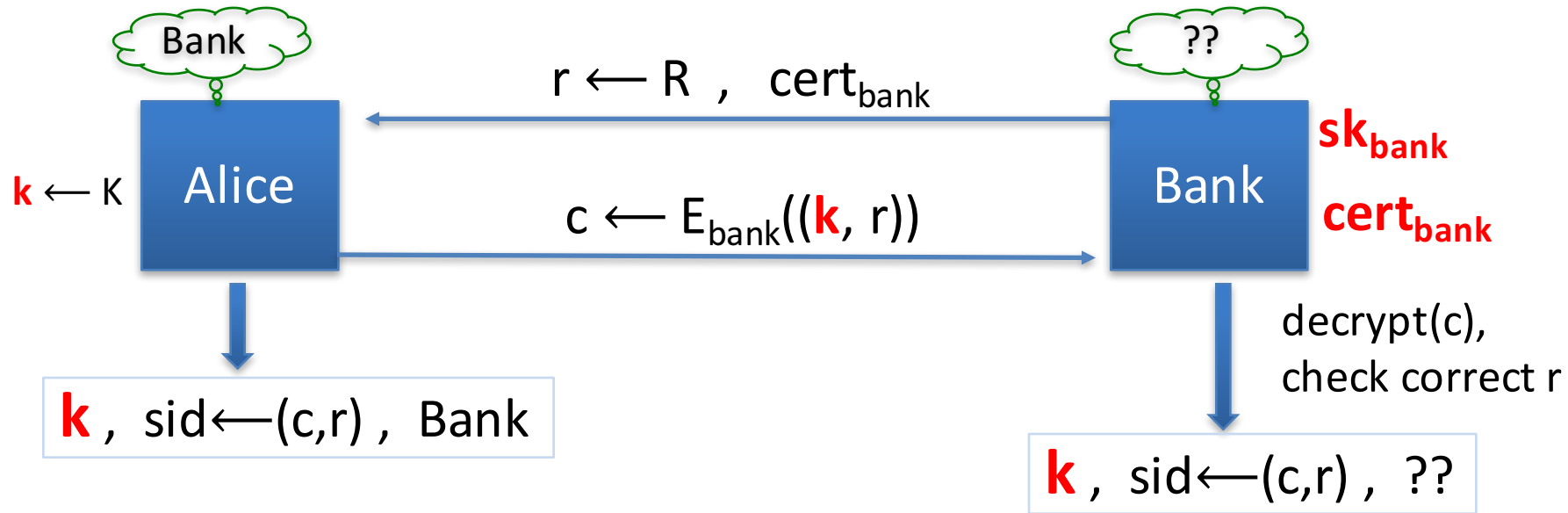
- Recall: from  $E_{\text{bank}}((m,r))$  adv. cannot build  $E_{\text{bank}}((m,r'))$  for  $r' \neq r$

$S_{\text{alice}}((m,r)) = S(sk_{\text{alice}}, (m,r))$  where  $S$  is a signing algorithm

**R**: some large set, e.g.  $\{0,1\}^{256}$

# Protocol #1

# Simple one-sided AKE protocol

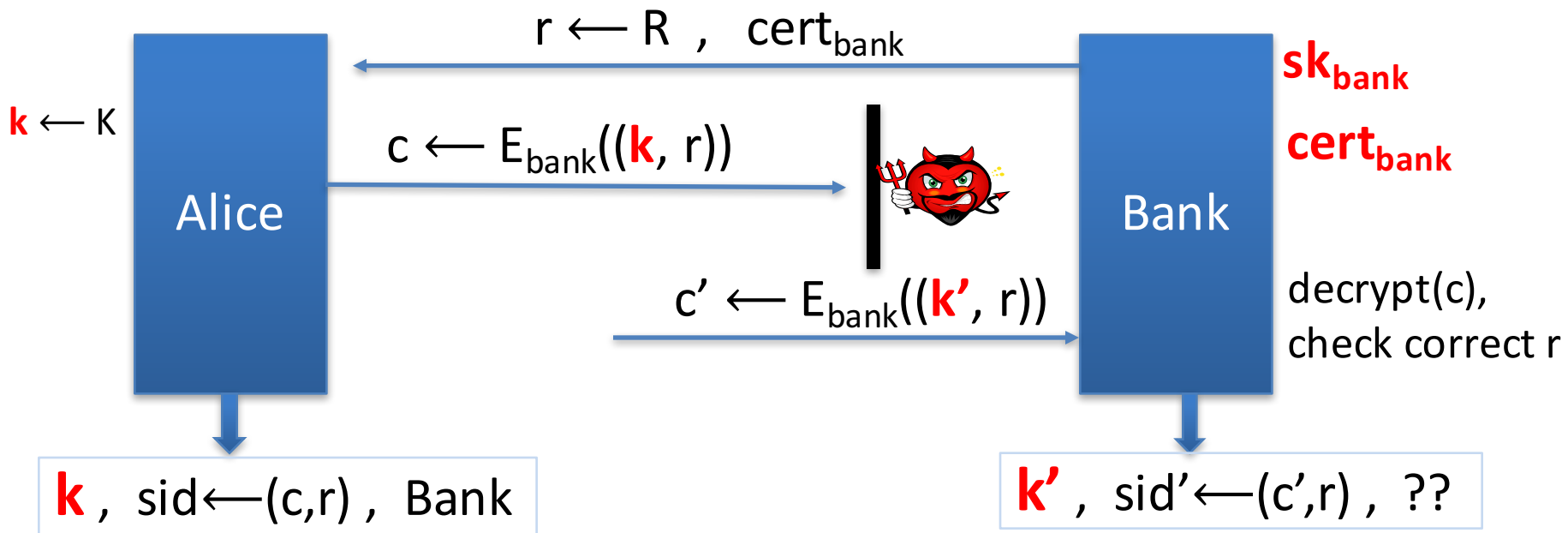


“Thm”: this protocol is a secure one-sided AKE

Informally: if Alice and Bank are not corrupt then we have  
(1) secrecy for Alice and (2) authenticity for Alice

# Did the AKE complete successfully?

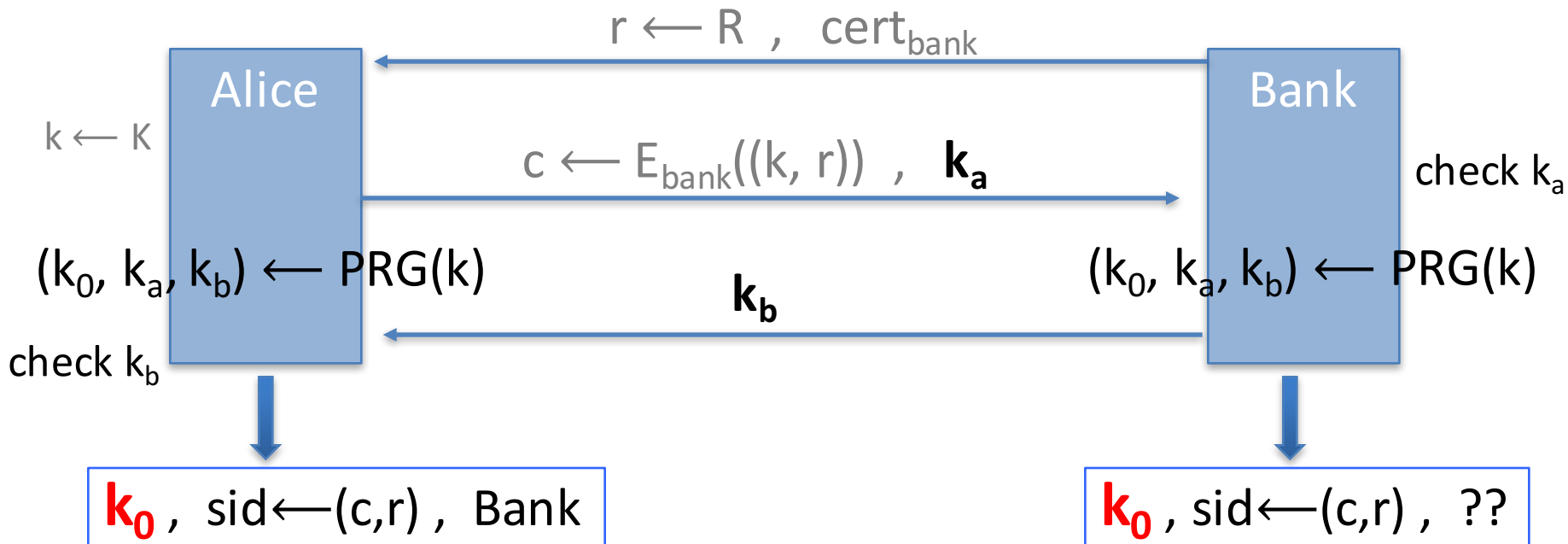
Problem: Alice does not know if Bank received  $k$



**One-sided:** Bank does not know who  $k'$  is shared with

# Explicit AKE via key confirmation

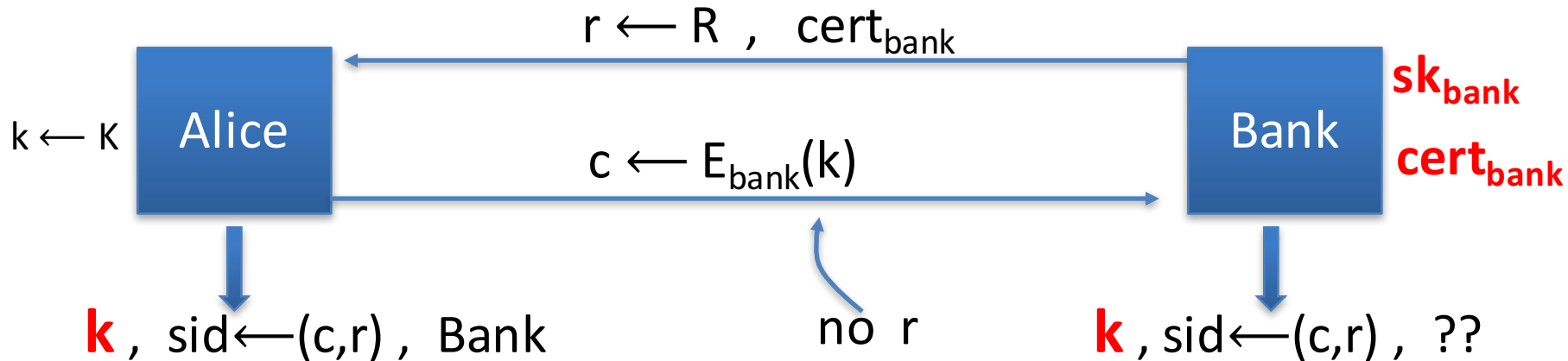
Key confirmation: if succeeds, Alice is assured Bank has  $k$ .



Note:  $k_0$  used as session key (not  $k$ )

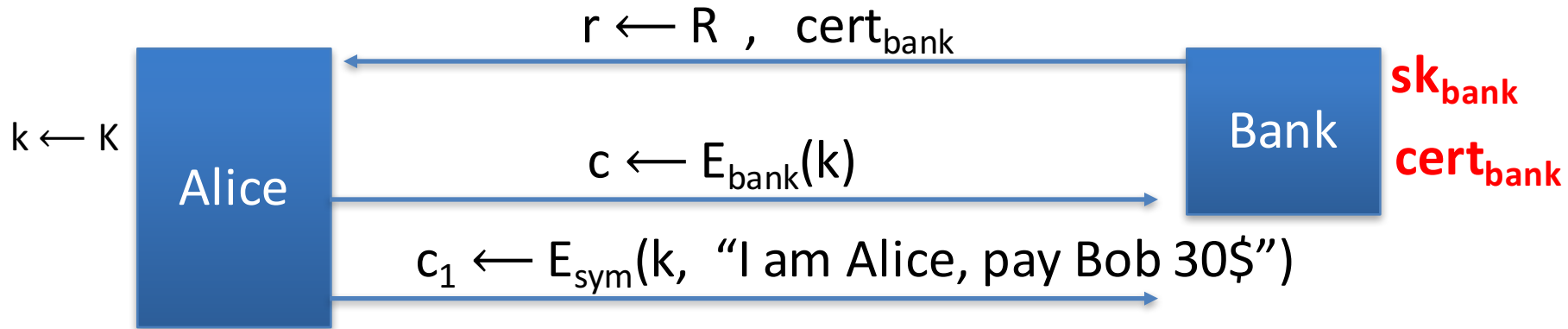


# Insecure variant 1: $r$ not encrypted

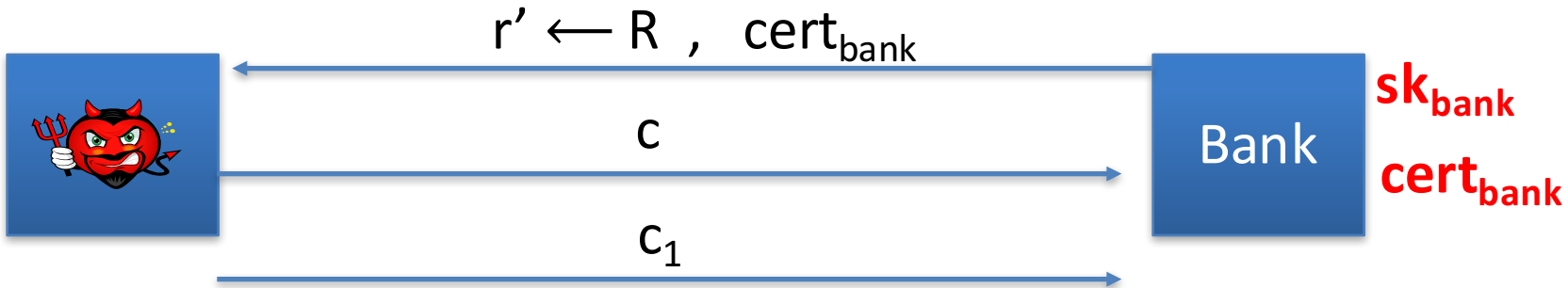


Problem: replay attack

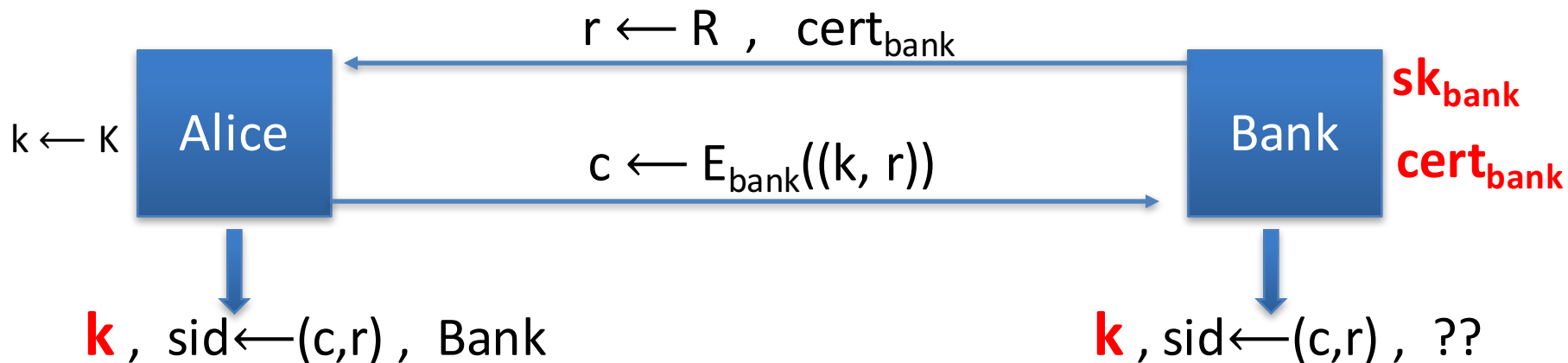
# Replay attack



Later:



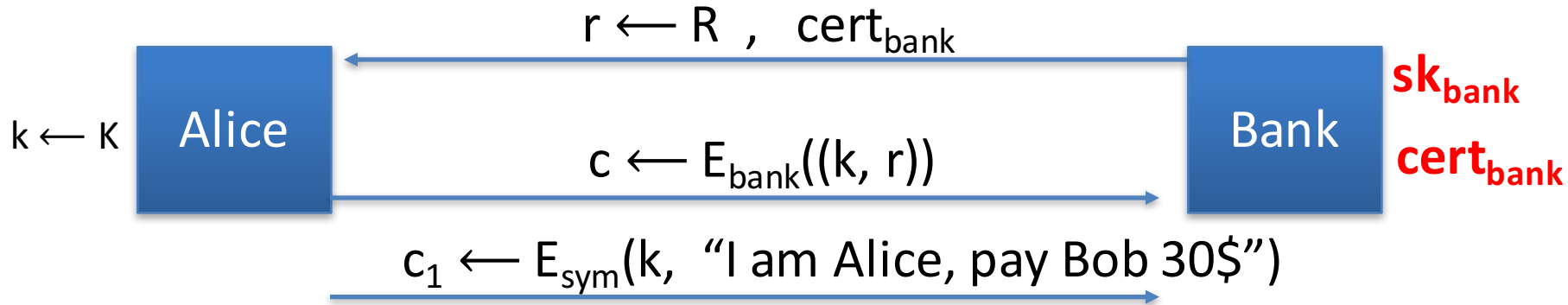
# Insecure variant 2: $E_{\text{bank}}$ not CCA-secure



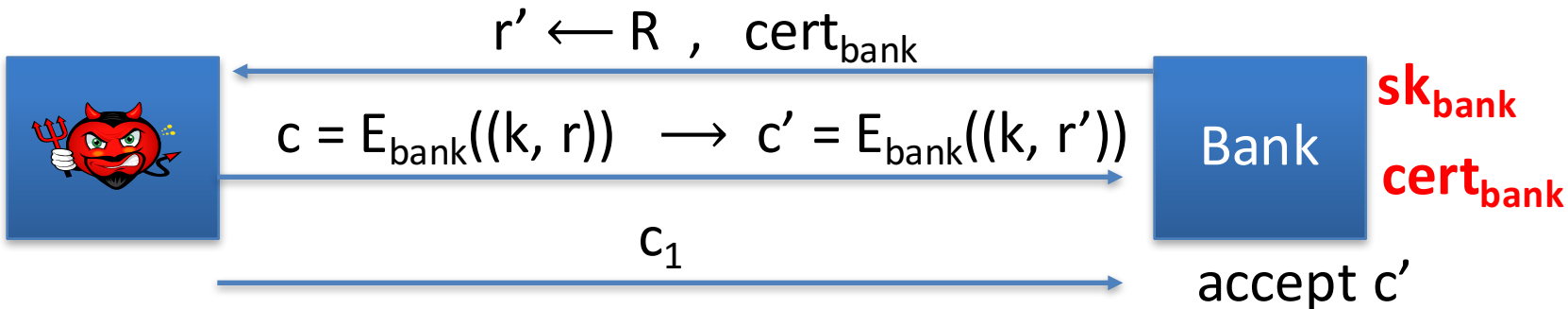
Suppose: from  $c = E_{\text{bank}}((k, r))$  can construct  $c' = E_{\text{bank}}((k, r'))$  for any  $r'$

$\Rightarrow$  replay attack

# Replay attack

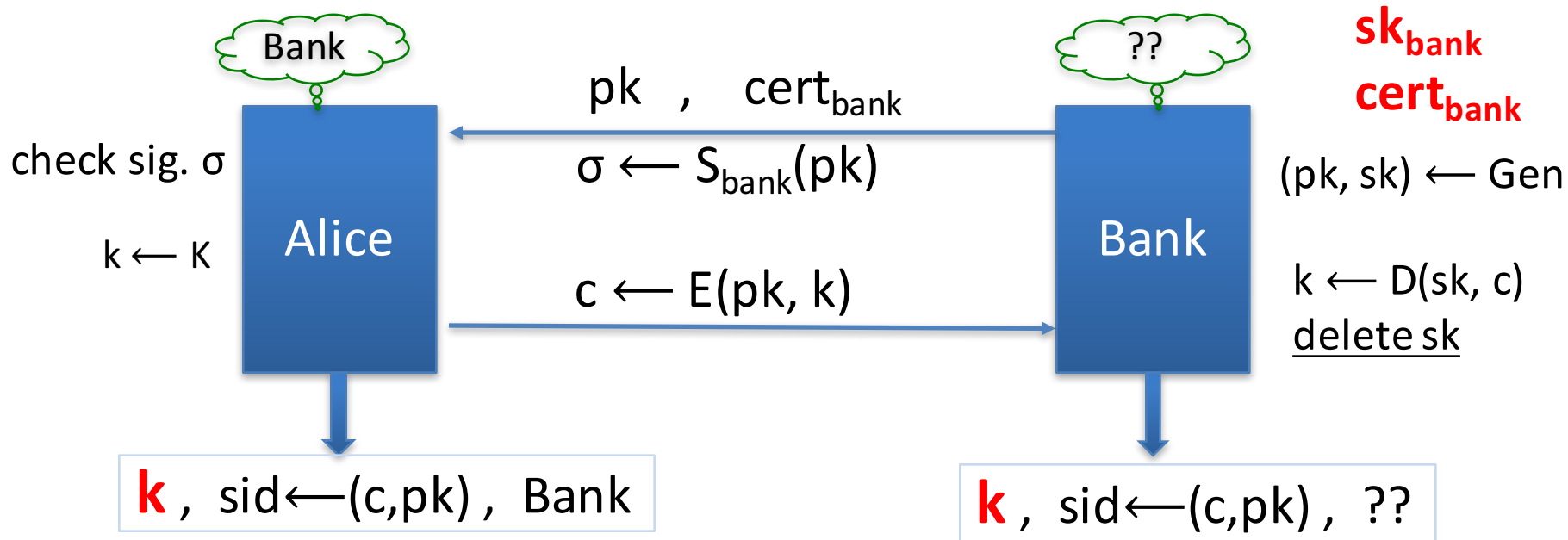


Later:



# Protocol #2

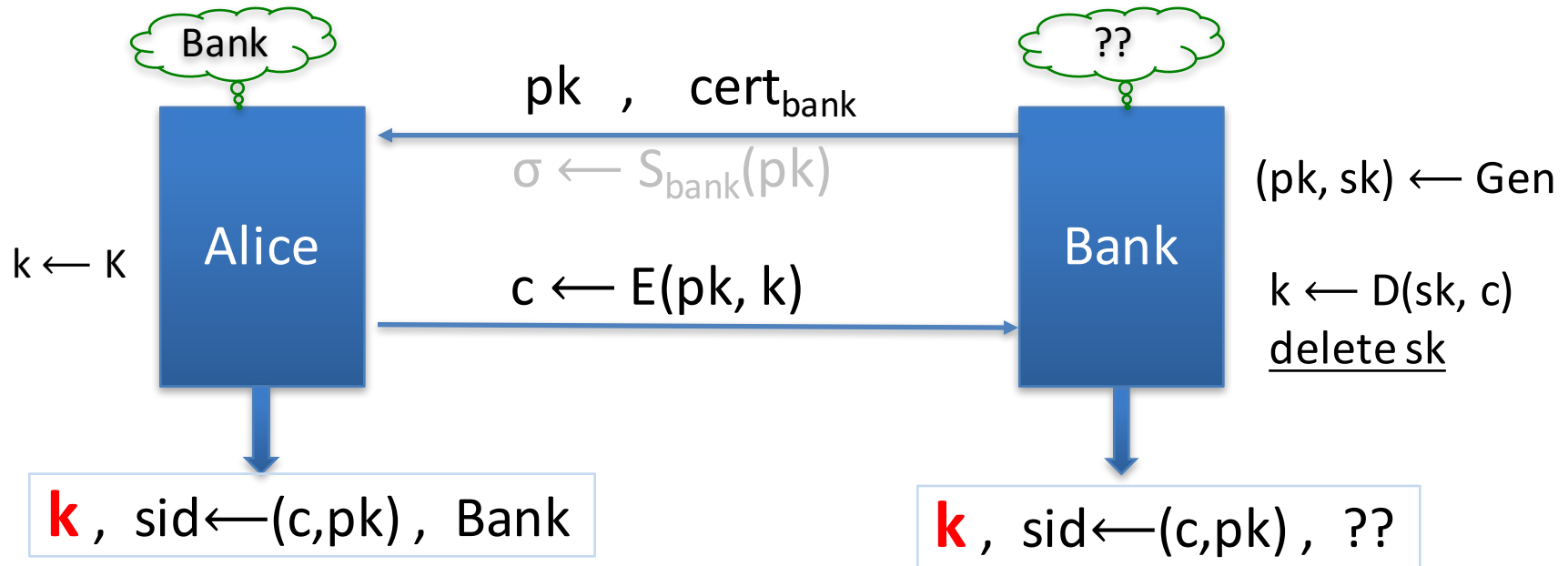
# Simple one-sided AKE with forward-secrecy



$(pk, sk)$  are ephemeral:  $sk$  is deleted when protocol completes

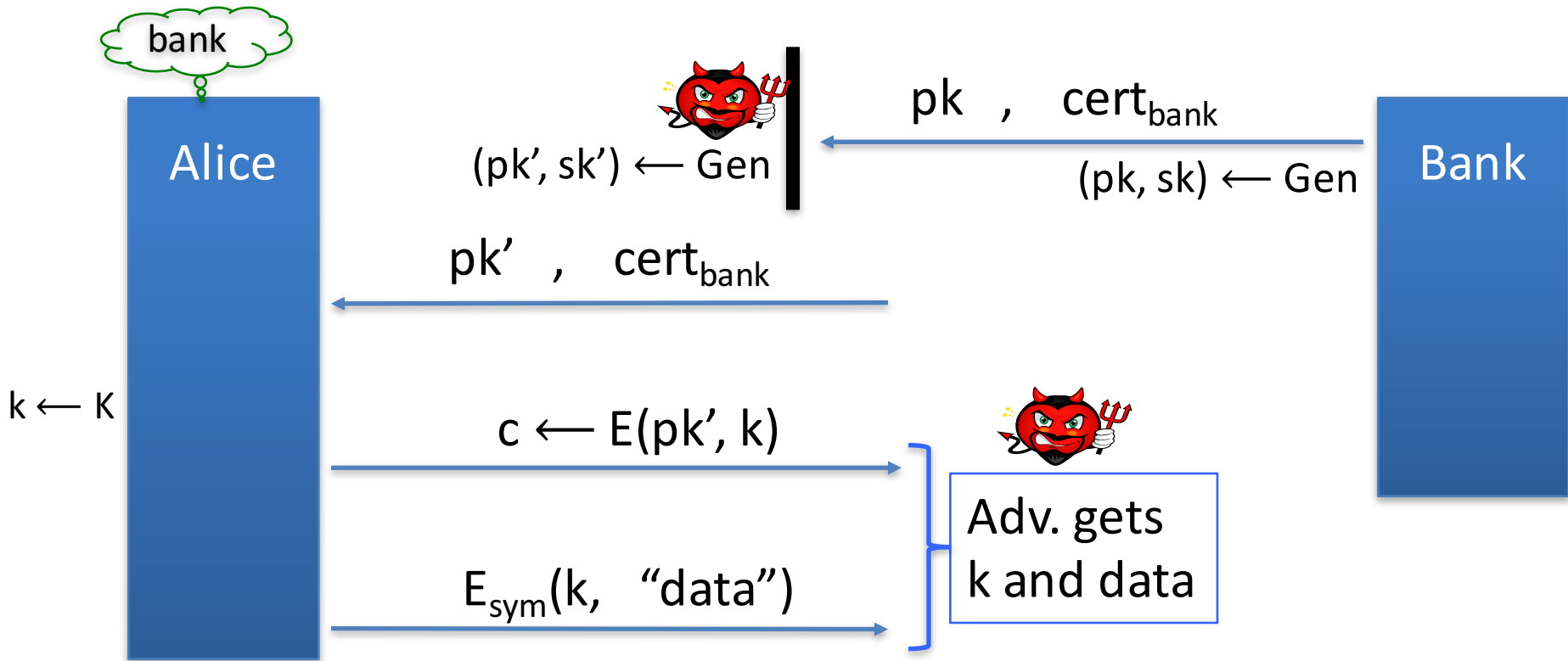
Compromise of Bank: past sessions are unaffected

# Insecure variant: do not sign pk



Attack: complete key exposure

# Attack: key exposure

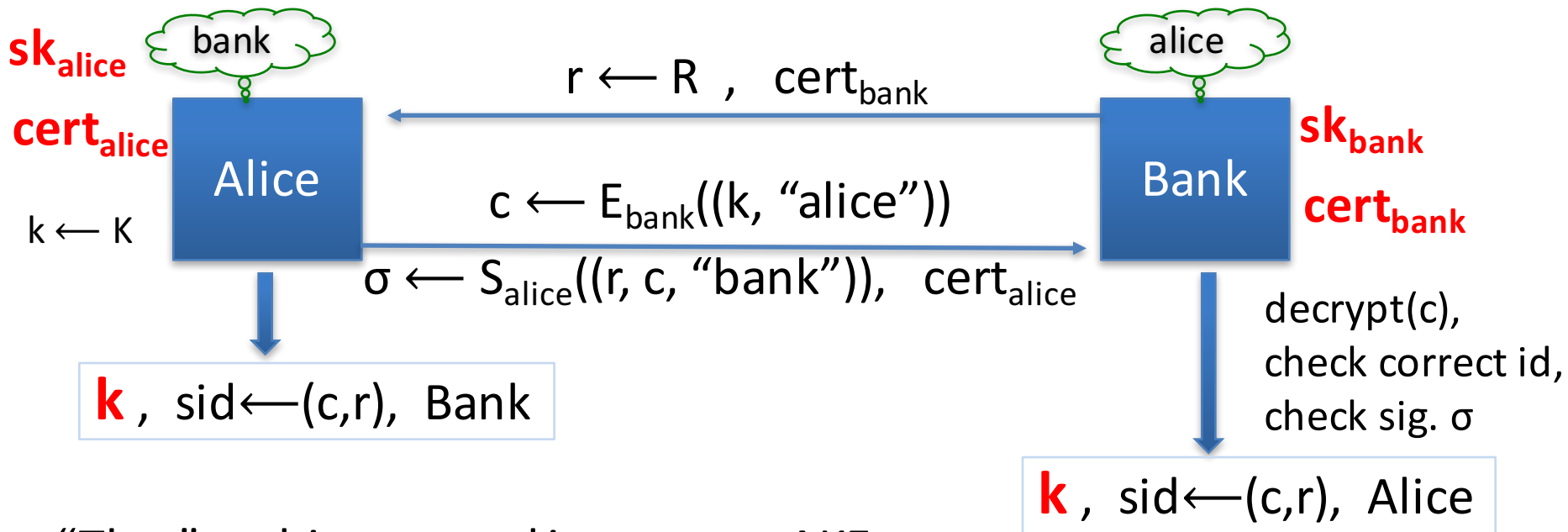




# Two-sided AKE

For now: no forward secrecy

# Two-sided AKE (mutual authentication)



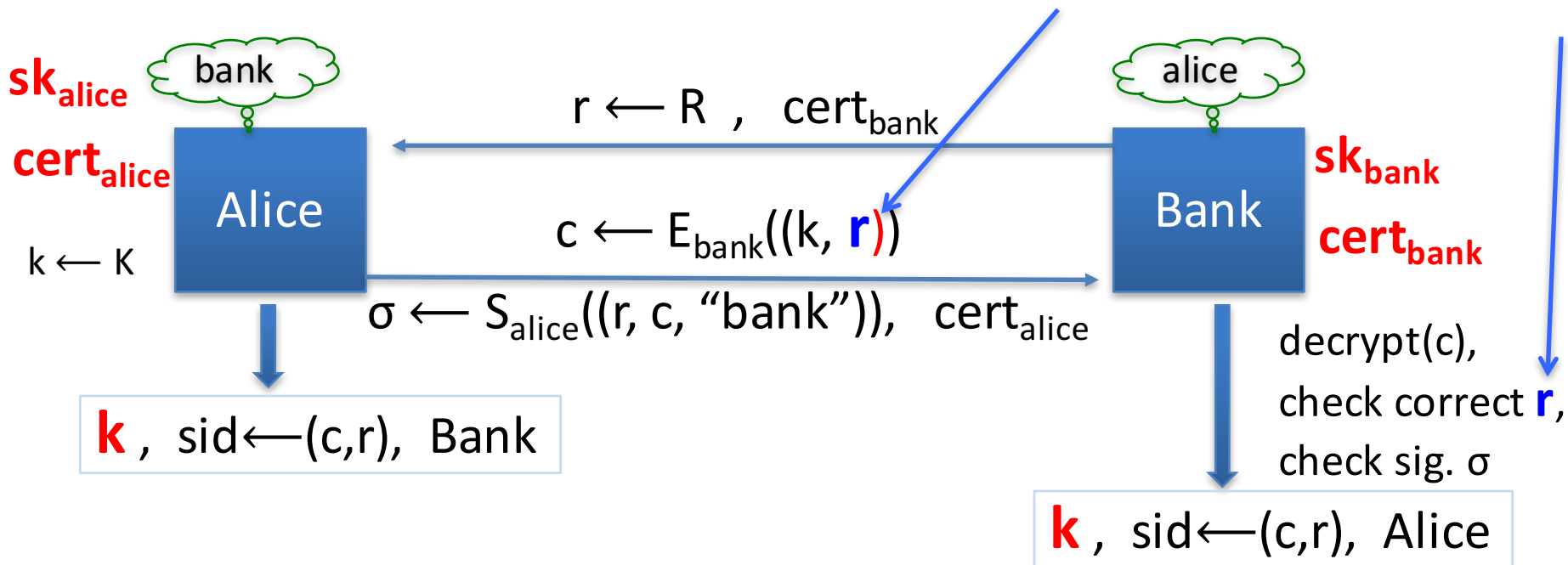
“Thm”: this protocol is a secure AKE

Informally: if Alice and Bank are not corrupt then we have  
 (1) secrecy and (2) authenticity for Alice and for Bank

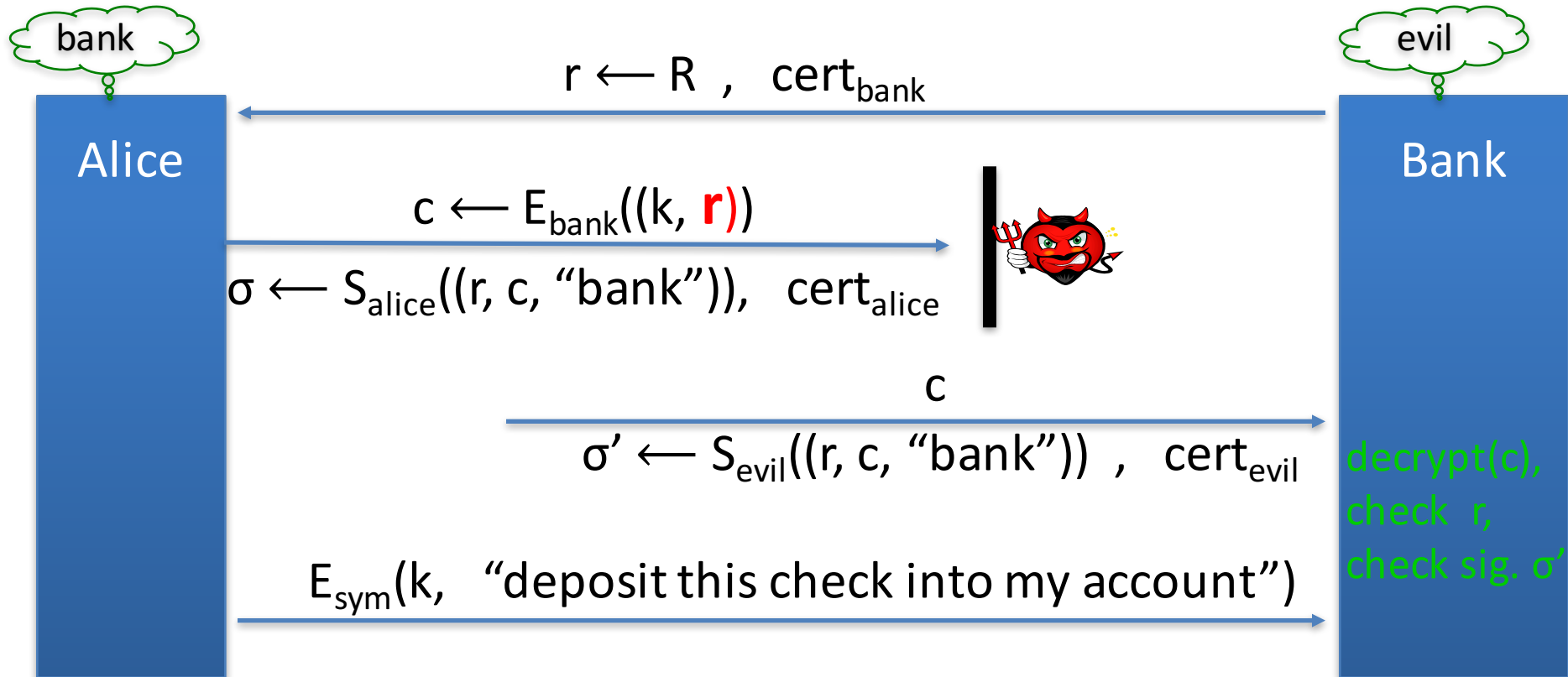
# Insecure variant: encrypt **r** instead of “Alice”

Any change to protocol makes it insecure, sometime in subtle ways

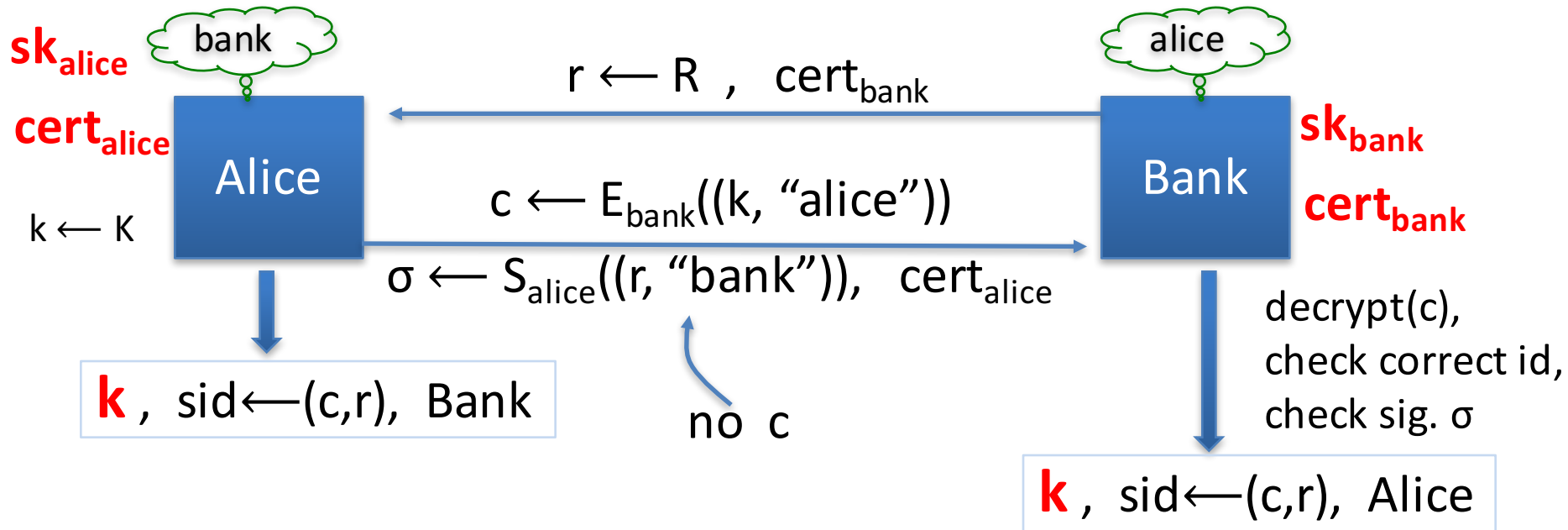
Example:



# Attack: identity misbinding

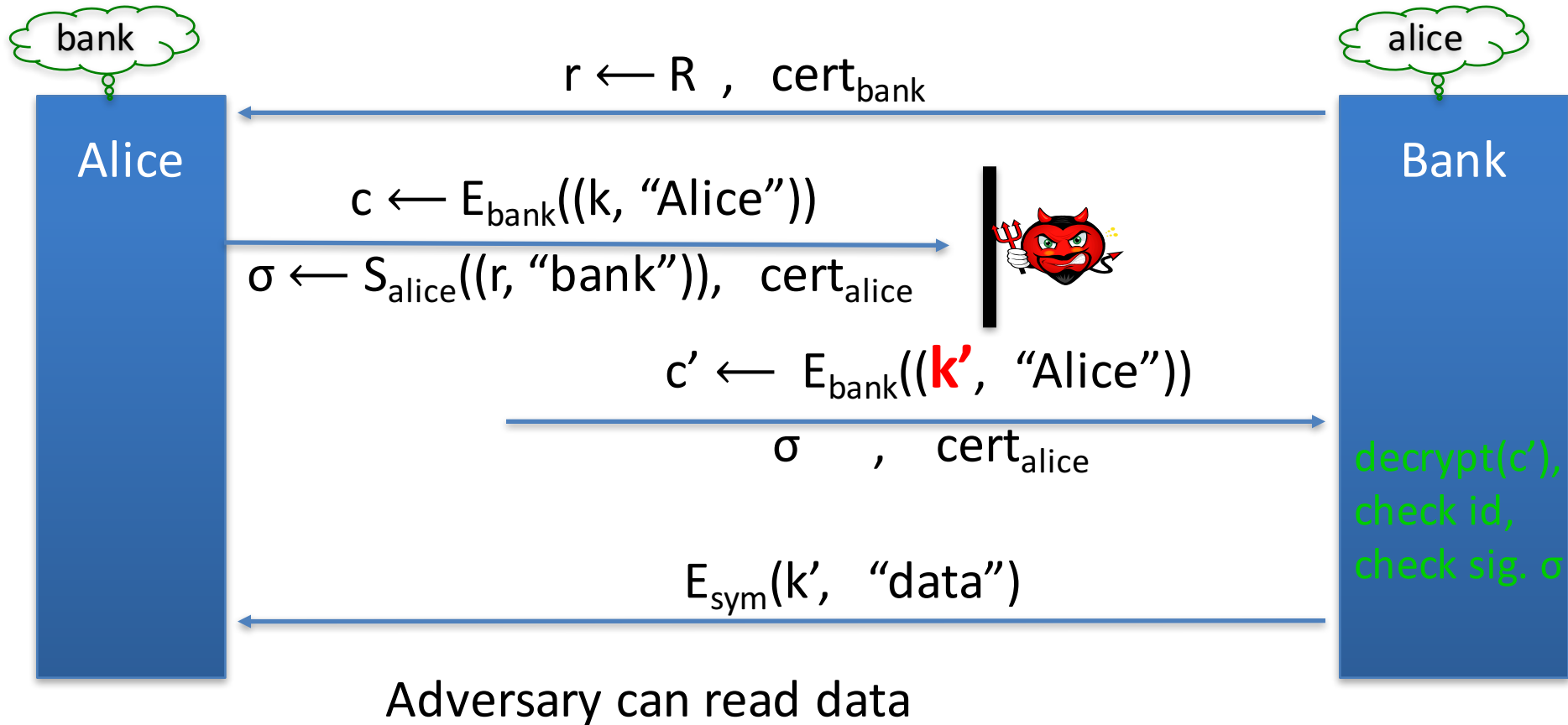


# Insecure variant: do not sign c

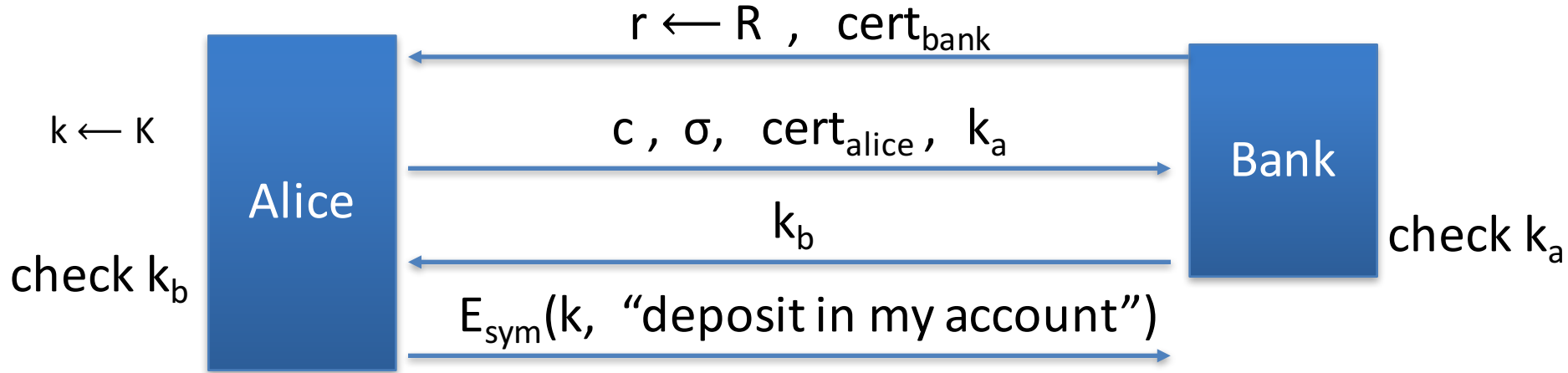


Attack: key exposure

# Attack: key exposure



Can we defeat the attack on previous slide with key confirmation?



Yes, the attacker does not know  $k$  and cannot send a valid  $k_b$

# Many more AKE variants

Two-sided AKE with forward secrecy:

AKE with end-point privacy:

- Goal: certificates are not visible to adversary (TLS 1.3)

AKE based on a shared secret between Alice and Bank:

- High entropy shared secret: want forward secrecy
- Password: ensure no offline dictionary attack (PAKE)



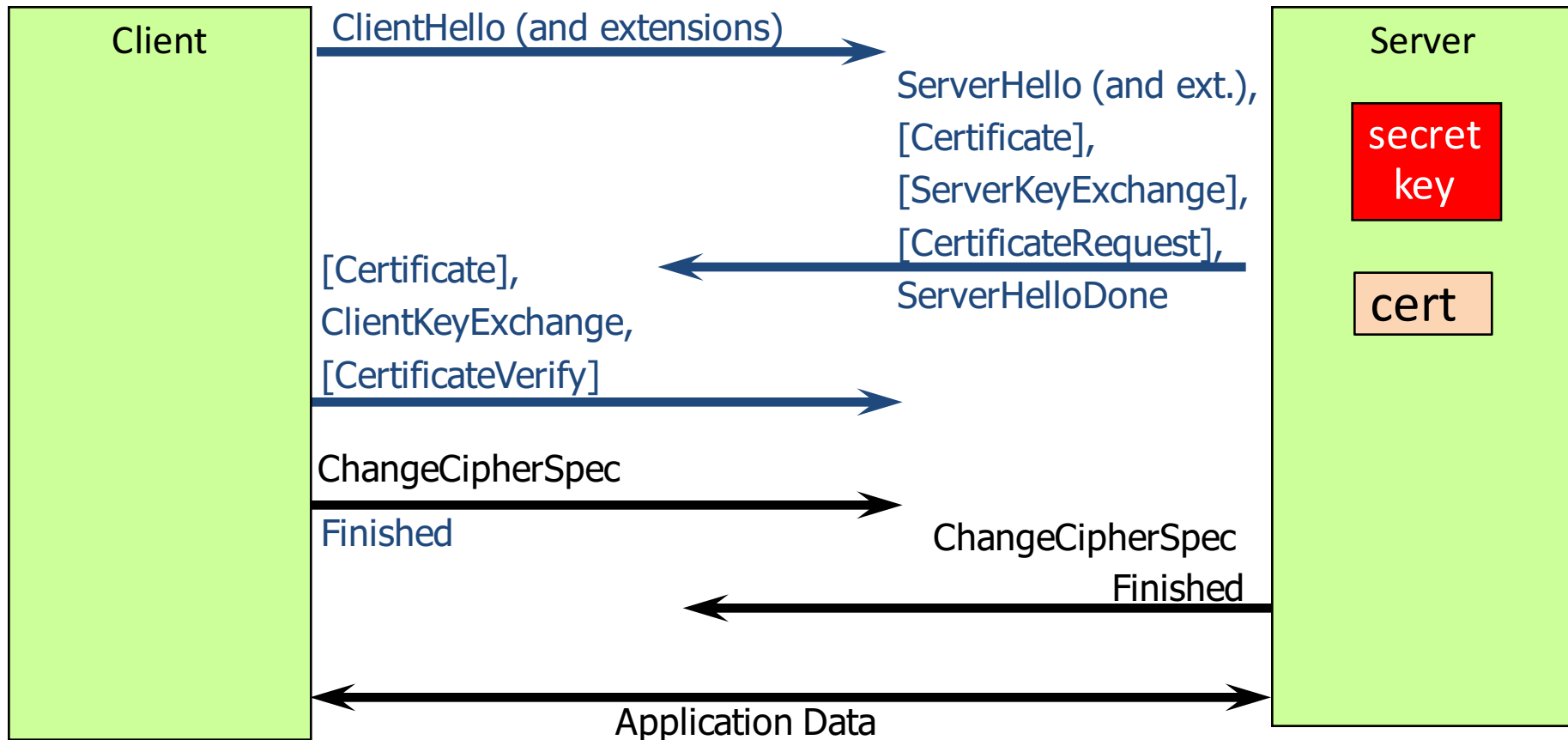


Auth. key exchange

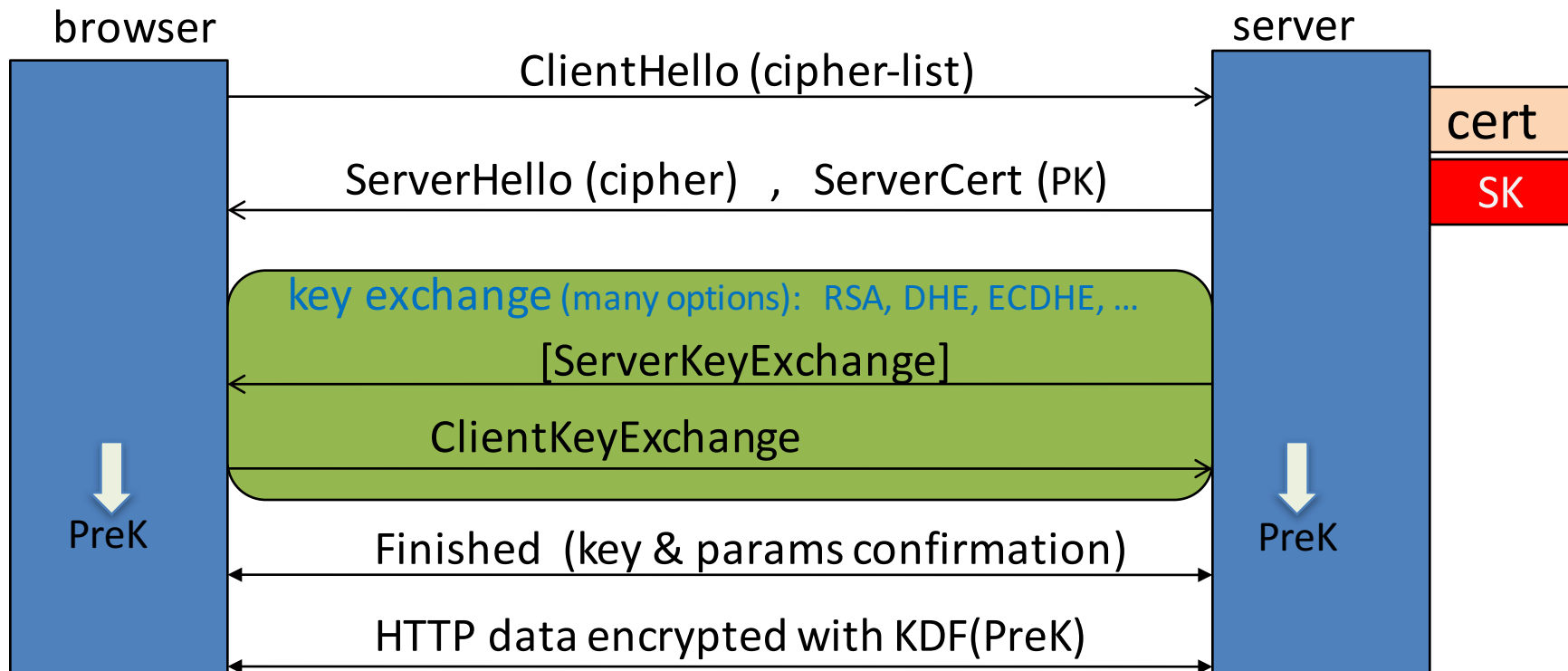
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TLS v1.2 key exchange

# TLS session setup (handshake)

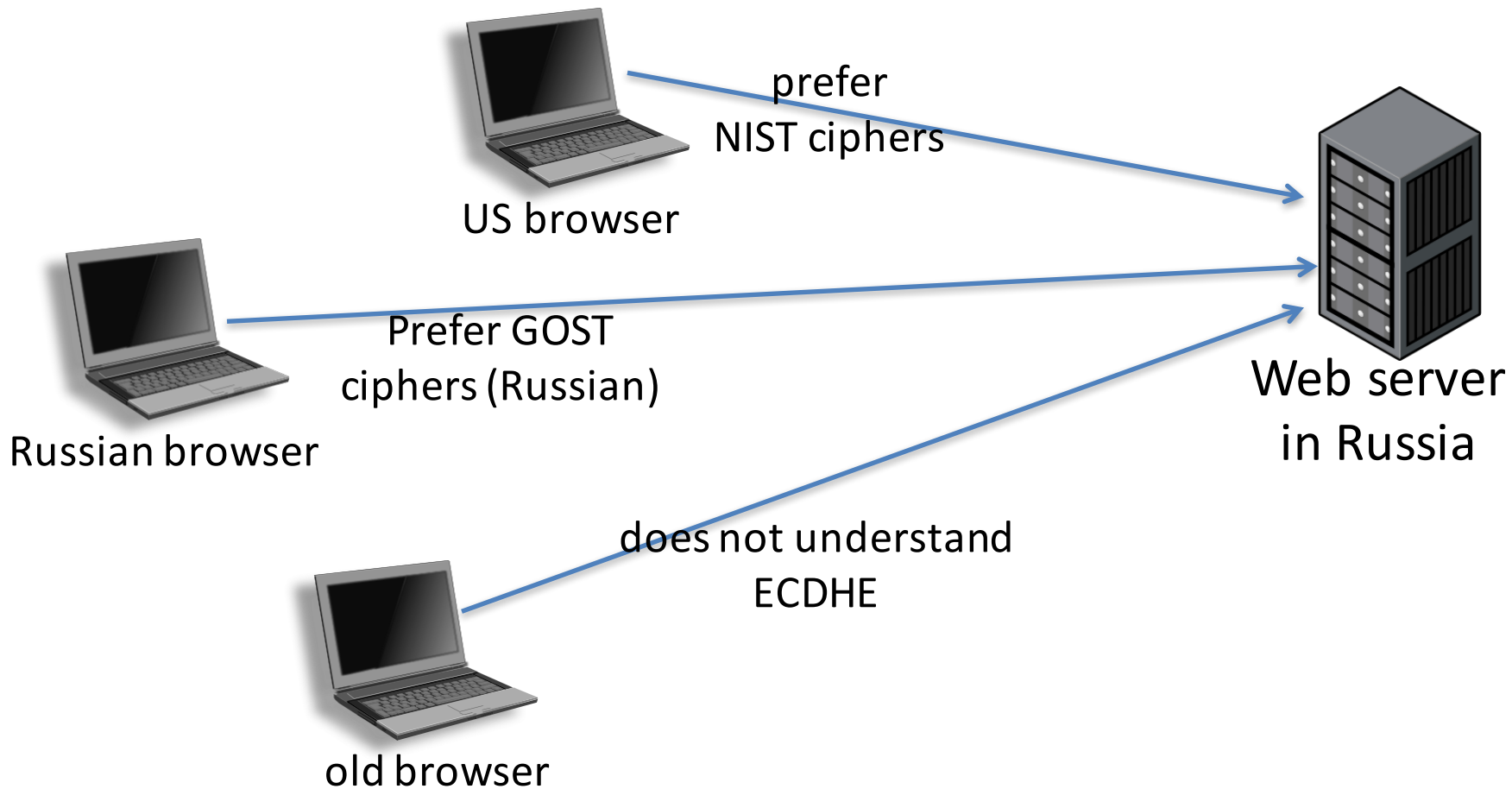


# Brief overview of SSL/TLS

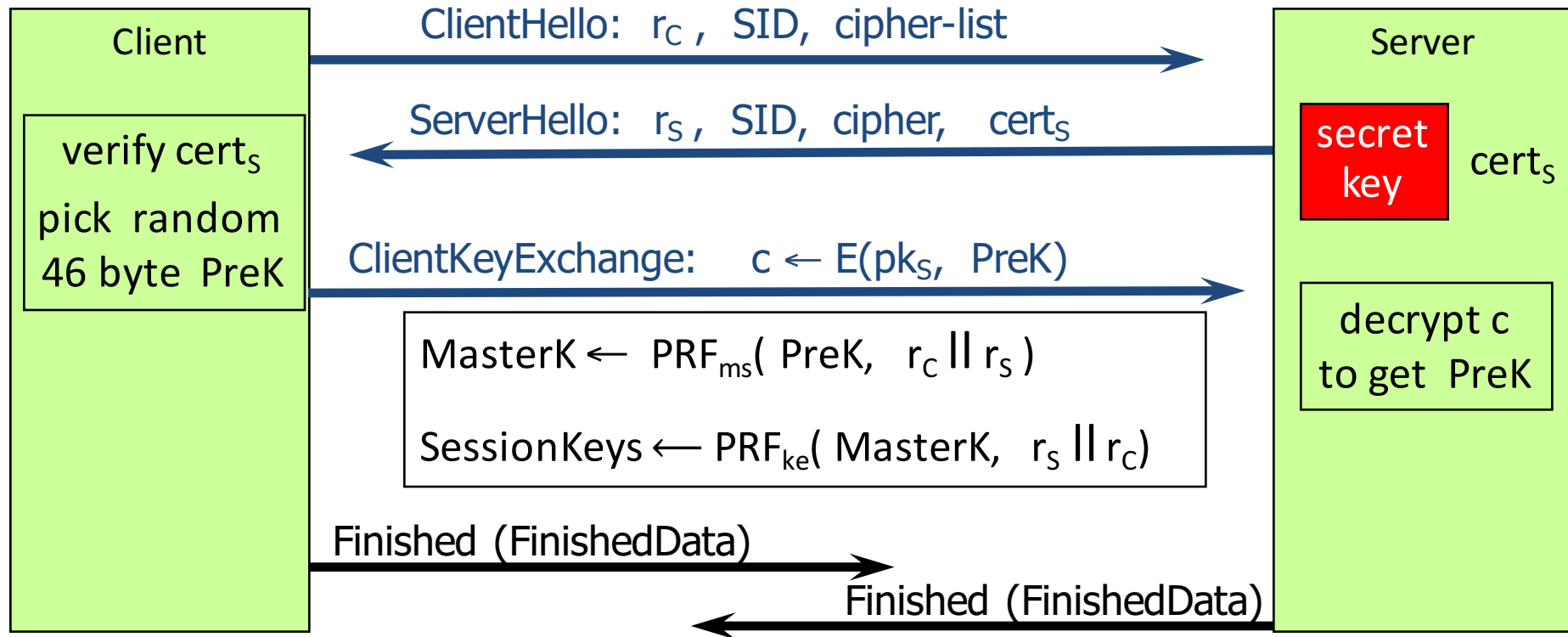


In this diagram: one sided authentication (no client authentication)

# The need for negotiating ciphers



# Abstract TLS: RSA exchange (simplified)



Key Confirmation:  $\text{FinishedData} = \text{PRF}_{\text{vd}}(\text{MasterK}, \text{hash}(\text{HandshakeMessages}))$

# Properties

$r_C, r_S$ : prevent replay of old session

## RSA key exchange: no forward secrecy

- Compromise of server secret key exposes old sessions
- Costly RSA decryption on server, easier RSA enc. on client

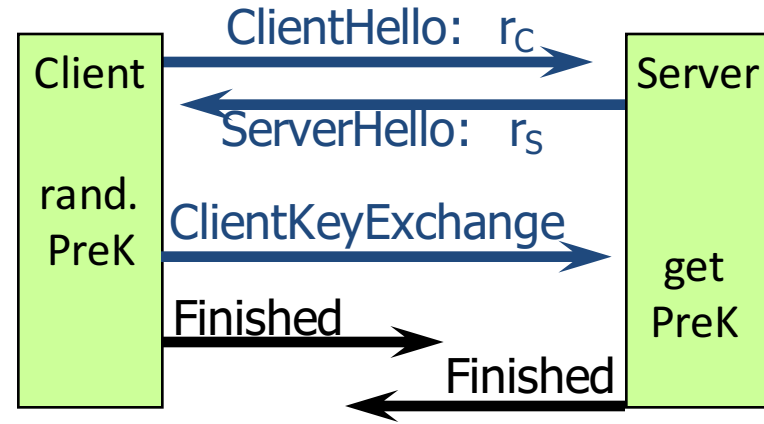
## One sided identification:

- Browser identifies server using server-cert
- Server has no guarantees about client's identity
  - TLS has support for mutual auth. (client needs  $sk_C$  and  $cert_C$ )



Suppose always  $r_C = 0$ , but  $r_S$  is random

Would this be a secure one-sided AKE?



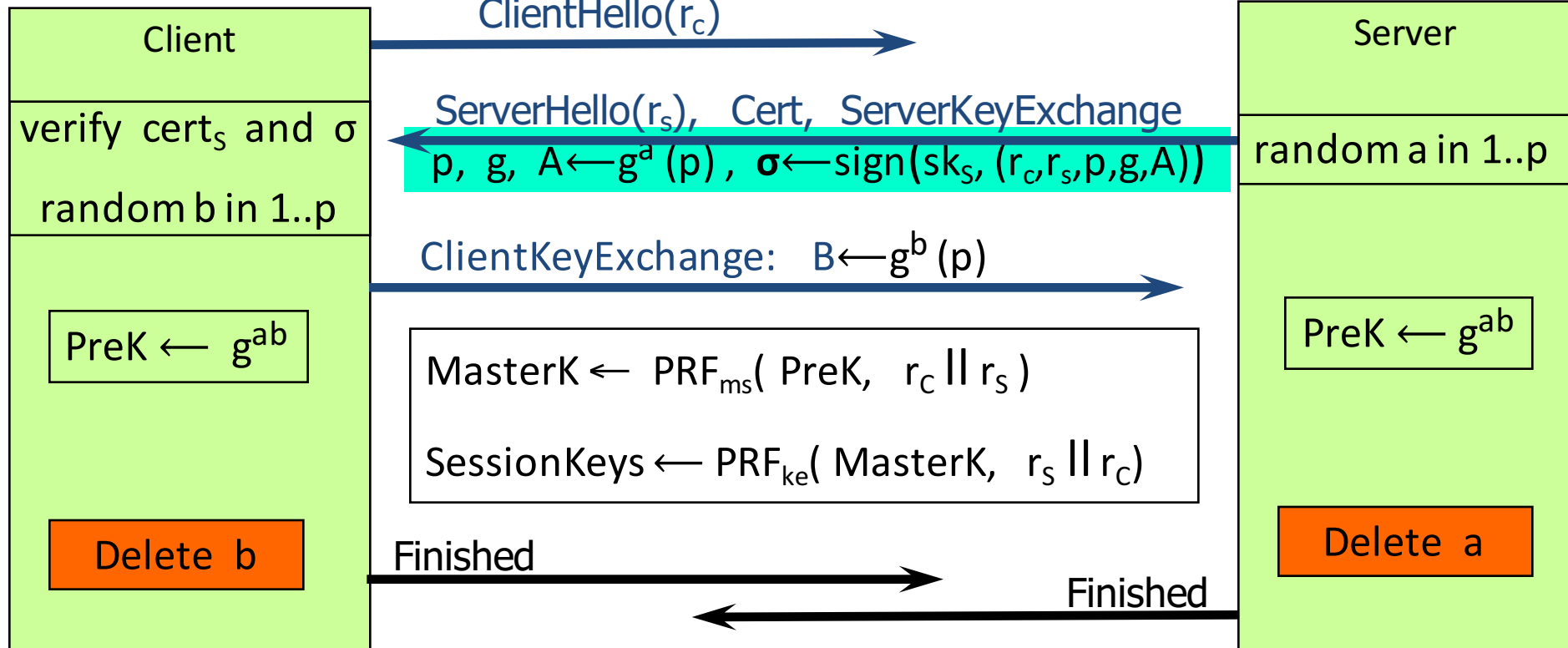
- No, an attacker can replay an old session to the server
- No, an attacker can replay an old session to the client
- Yes, it would be a secure one-sided AKE
- No, a man in the middle can expose PreK

# TLS key exchange with forward-secrecy (DHE)

(simplified)

Fix prime  $p$  and  $g$

$sk_S$ : signing key







**www.google.com**

The identity of this website has been verified by Thawte SGC CA.

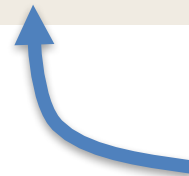
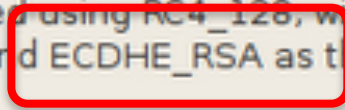
[Certificate Information](#)



Your connection to www.google.com is encrypted with 128-bit encryption.

The connection uses TLS 1.0.

The connection is encrypted using RC4\_128, with SHA1 for message authentication and ECDHE\_RSA as the key exchange mechanism.



Elliptic curve  
Diffie-Hellman

Prefer ECDHE over DHE

# Performance: RSA vs. forward-secrecy

Cost of crypto operations on server per handshake:

- RSA key exchange: one RSA-2048 decryption (deprecated in TLS 1.3)
- ECDHE: Diffie-Hellman in group  $G$  with generator  $g \in G$

1. One exp. to compute  $A \leftarrow g^a \in G$

2. One sig. on Diffie-Hellman parameters  $(G, g, A)$

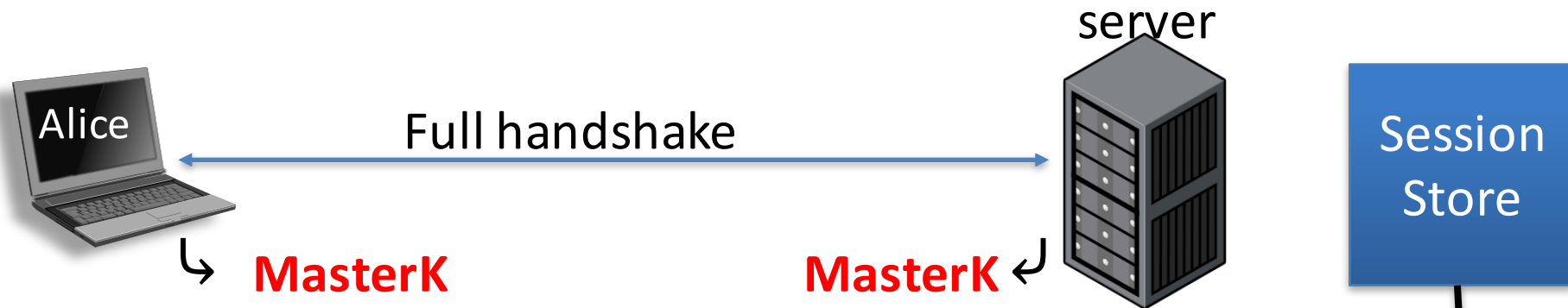
3. One exp. to compute DH secret:  $\text{PreK} \leftarrow g^{ab} \in G$

must be done  
for every  
handshake

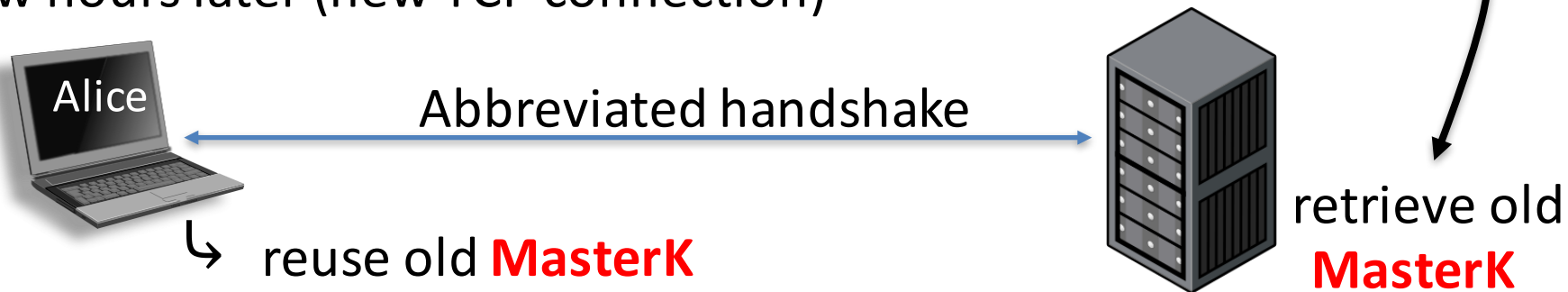
Server support (2014): RSA (99.9%), DHE (60%), ECDHE(18%)

# Session Resume

Goal: reduce # of full handshakes



Few hours later (new TCP connection)



# Session resume (simplified)

Client

**MasterK(bank)**

$SID_C=0$ : full handshake

$SID_C \neq 0$ : resume old session

If  $SID_C = SID_S$   
then resume  
else full

ClientHello:  $r_C, SID_C$

$SID_S \leftarrow SID_C$  if  $SID_C \in ST$

$SID_S \leftarrow \text{random}$ , otherwise

ServerHello:  $r_S, SID_S$

SessionKeys  $\leftarrow \text{PRF}_{ke}(\text{MasterK}, r_S \parallel r_C)$

ChangeCipherSpec

Finished

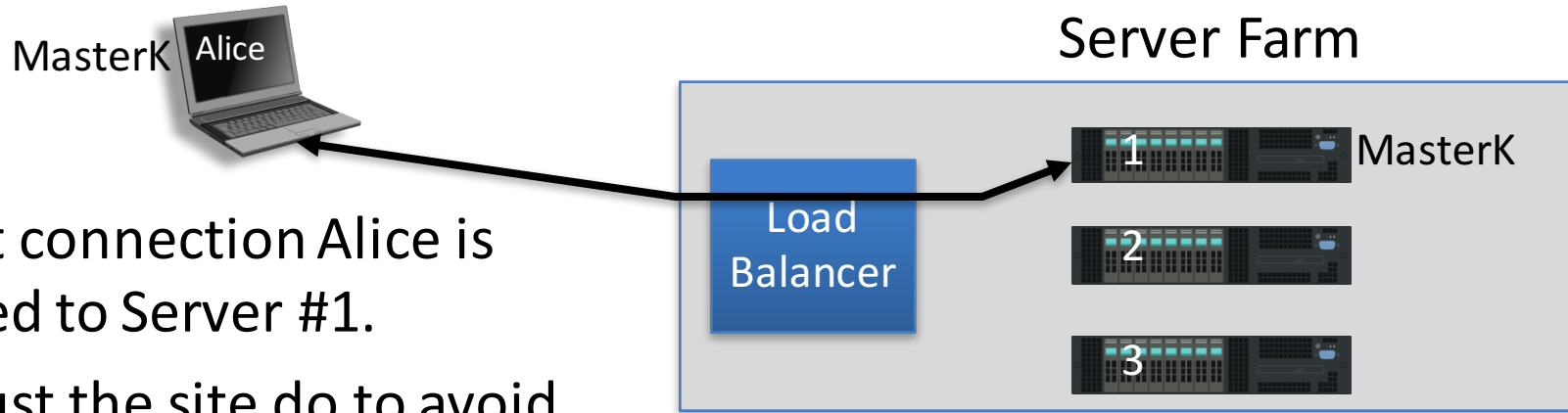
ChangeCipherSpec

Finished

Bank

Session Store (ST)

**MasterK(Alice)**



On a first connection Alice is connected to Server #1.

What must the site do to avoid a full handshake on subsequent connections from Alice?

- Ensure that Alice always connects to server #1
- Ensure that SessionStore is shared among all servers in farm
- Do all TLS processing in the load balancer
- All of the above are reasonable solutions

THE END