So Who Won? Dynamic Max Discovery with the Crowd

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Outline

- Why Crowdsourcing?
- Finding Maximum
 - Judgement Problem
 - Next Votes Problem
- Conclusion
- References

Why Crowdsourcing?

To solve problems that are difficult for computers

- Sort / Max [1]
- Graph search [5]
- Categorize [4]
- Filter [3]

- Tradeoffs [3]
- Latency
- Cost
- Uncertainty

Why Crowdsourcing?

To solve problems that are difficult for computers

• Sort / Max [1] < focus of this talk

Tradeoffs [3]

- Graph search [5] Latency
- Categorize [4]
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- Cost
- Uncertainty

Closest point?



Best profile picture?



Best profile picture?





Best profile picture?



Max Problem

- Goal: Find object with maximum *quality*
- How: ask pairwise comparisons votes
- Workers vote correctly with probability *p*
- Variants
 - Structured
 - Unstructured

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• Unstructured

Unstructured setting

- Judgement Problem: what is our current best estimate for the overall max winner?
- Next Votes Problem: how to choose most effective votes to invoke, given current standing?

Unstructured setting

Both problems are:

- NP-Hard < why? see [1] for details
- Good heuristics exists! #phew
 - More on this soon

Judgement Problem

Current best estimate for the overall max winner?

Representation: weighted directed graphs



ML Formulation

Let π denote a permutation function

For object i, $\pi(i)$ denotes its rank

$$P(\boldsymbol{\pi}^{-1}(k) = j | W) = \frac{\sum_{d: \pi_d^{-1}(k) = j} P(W | \pi_d)}{\sum_l P(W | \pi_l)}$$

ML Formulation: Given W and p, determine:

$$\arg\max_{j} P(\boldsymbol{\pi}^{-1}(1) = j|W)$$

Heuristic Strategies

- Indegree Strategy
- Local Strategy
- PageRank Strategy
- Iterative Strategy

Indegree Strategy

- Need to know worker accuracy *p*
- Scoring function represents number of in-degrees
- Transform graph such that I(i,j) + I(j,i) = 1
- $I(j,i) = P(\pi(i) < \pi(j) | w(i,j), w(j,i))$
- Find node with highest sum of in-degree weights

Local Strategy

Use local evidence

$$egin{aligned} wins(i) &= \sum_j w_{ji} \quad losses(i) &= \sum_i w_{ij} \ s(i) &= wins(i) - losses(i) + \sum_j \left[\mathbf{1}(w_{ji} > w_{ij}) wins(j)
ight] \ &- \sum_j \left[\mathbf{1}(w_{ij} > w_{ji}) losses(j)
ight] \end{aligned}$$

We now consider evidence 2 steps away

PageRank Strategy

Use global evidence

$$pr_{t+1}(i) = \sum_{j} \frac{w_{ji}}{d^+(j)} pr_t(j) \qquad d^+(i) = \sum_{j} w_{ij}$$

The probability masses concentrate on the Strongly Connected Components

Subtle differences from original PageRank

Does not converge. How to handle this?

Iterative Strategy

Rank objects using a scoring metric (which one?)

Remove lower ranked objects

Repeat until final object is obtained

Any metric can be used

Iterative Strategy

Rank objects using a scoring metric (which one?)

Remove lower ranked objects

Repeat until final object is obtained

Any metric can be used, eg: wins(i) - losses(i)

Comparison

Heuristic	Prediction
ML	(D, C, B, A) and (C, D, B, A)
Indegree	(D, C, B, A)
Local	(D, C, B, A)
PageRank	Maximum object = C
Iterative	(C, D, B, A), (C, D, A, B), (D, C, B, A), or
	(D, C, A, B)

- ML has best performance
- Iterative is best when votes sampled are high
- PageRank bad with low worker accuracy
- PageRank best when votes sampled are low, with high worker accuracy



Next Votes Problem

Given current standing and an additional vote budget b, what votes to invoke?

Adaptive v One-shot



$$W = \left(\begin{array}{rrrrr} 0 & 2 & 0 & 0 \\ 0 & 0 & 2 & 3 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{array}\right)$$

ML Formulation

Q: a vote multiset; |Q| = b

A(Q): corresponding answer multiset for Q

$$P_{max}(a \wedge W) = \max_{i} P(\boldsymbol{\pi}^{-1}(1) = i | a \wedge W)$$

ML Formulation: Given b, W and p, determine Q, that maximizes:

$$\sum_{a \in A(Q)} \max_{i} P(\boldsymbol{\pi}^{-1}(1) = i, a \wedge W)$$

Evaluation

We use the following framework to evaluate additional votes:

- Use W to score all objects with a scoring function
- Select a batch of *b* votes to request
- Compute new scores and find maximum object

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Heuristic Strategies

- Paired Vote Selection
- Max Vote Selection
- Greedy Vote Selection



Complete Tournament Vote Selection

Paired Vote Selection

- Greedy
- No object chosen twice
- Performs well when objects have similar scores
- Good/bad why?



Max Vote Selection

- More focus on find top ranked object
- Should be better than Paired Vote
- Good/bad why?



Greedy Vote Selection

- Find product of scores of pairs
- Choose *b* highest weighted pairs
- Good/bad why?



Complete Tournament

- Take top K objects
- Do round-robin among them (choose K accordingly)
- Given K, should we choose an even lower value? Why?
- Good/bad why?



- ML-ML has best performance
- Prediction performance increases with *b* (concave)
- Prediction performance increases with p (convex)
- Complete Tournament and Greedy are clear winners



Greedy v Complete Tournament

- Objects of different types
- Initial votes across same types more likely
- We assume no initial votes across different types
- Complete Tournament is the winner
- Complete Tournament works better with fewer objects





 Complete Tournament is the winner

•

 Complete Tournament works better with fewer objects



Discussion

- Can the first round of votes be invoked better?
- Theoretical basis for the behavior of heuristics
- Why does PageRank work well with fewer initial votes?
- Why is Complete Tournament better than Greedy?

Conclusion

- Judgement Problem
- Next Votes Problem
- Effective Heuristics
 - PageRank
 - Complete Tournament

References

[1] So who won?: dynamic max discovery with the crowd, S Guo, A Parameswaran, H Garcia-Molina

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[4] Human-assisted Graph Search: It's Okay to Ask Questions. Aditya Parameswaran, Anish Das Sarma, Hector Garcia-Molina, Neoklis Polyzotis and Jennifer Widom

[5] Active Sampling for Entity Matching. Kedar Bellare, Suresh Iyengar, Aditya Parameswaran and Vibhor Rastogi

Questions?



THANKS FOR LISTENING AND **KEEP** CLAPPING